# **"Anti" CHSH inequality - natura facit saltus.**

## **Ilija Barukčić** \*, 1

<sup>1</sup> DE-26441 Jever. Germany. http://www.barukcic-causality.com/

#### *Abstract*

The relation between the hidden and non-hidden part of something is not without conflicts. The one is the hidden, the other the non-hidden, but equally both are only as separated in the same relation, each excludes thus the other from itself. The one is in relation with itself by its other and contains the same. It is thus the whole, self-contained opposition. The one is without its other, the hidden is not the non-hidden and vice versa, the hidden excludes from itself the non-hidden and thus at the end its own self, each side in its own self excludes itself. It is quite clear that both are opposed to each other. This lack can be taken as their determinateness. The one that has within itself the difference from itself changes under certain conditions. The quantitative alteration of something has a range within it remains indifferent to any alteration, it is indifferent towards the other of itself. Under this circumstances, the something does not change its quality at all. Only, there is always a point in this quantitative alteration of something at which the quality of that something is changed, the quantum shows itself as specifying, the point of no return is reached, natura facit saltus. The altered something converts itself into a new quality, into a negation of a negation, into a new something. The new something is subject of the same alteration and so on to infinity. This publication will proof, that

**the CHSH inequality is not compatible with**

#### **Einstein's General Relativity and**

#### **Heisenberg's uncertainty principle.**

*Key words:* Change, Natura facit saltus, CHSH inequality, Einstein, Heisenberg, General contradiction law, Barukčić.

# **1. Introduction**

The CHSH inequality was derived by John Clauser, Michael Horne, Abner Shimony and Richard Holt in a very much-cited paper published in 1969 ( Clauser, 1969 )**.** The Clauser-Horne-Shimony-Holt (CHSH) inequality, an inequality of Bell's type, is as such related closely to Bell's theorem. Bell's (1964) theorem that bears his name is meanwhile proofed as a logical fallacy of the excluded middle (Barukčić 2006c, 2006d). Is the CHSH inequality besides of this still consistent with quantum mechanics and hiddenvariable theory with its underlying determinism? To say that the CHSH inequality is correct is to say that the same is compatible with Einstein and Heisenberg. For our present purposes the important point to recognise, in particular, is that, is there a disagreement between the CHSH inequality and Einstein and Heisenberg? However, it seems reasonable to suppose that it is difficult to advocate the CHSH inequality if there is a disagreement between the same and Einstein and Heisenberg. The question naturally arises, how can we proof, is the CHSH inequality compatible with Einstein and Heisenberg?

<sup>\*</sup> Corresponding author: e-mail: Barukcic@t-online.de. Phone: +00 49 44 61 99 11 11, Fax: +00 49 44 61 91 21 46. GMT +1h.

#### **2. Methods**

# **The CHSH inequality**

The original 1969 derivation of the CHSH inequality is not that much easy to follow. The usual form of the Clauser-Horne-Shimony-Holt (CHSH) inequality is known to be:

$$
-2 \leq (E(a, b) - E(a, b') + E(a', b) + E(a' b')) \leq +2
$$
  
or  

$$
-2 \leq S \leq +2
$$

where

 $L_{\text{L}}$ 



Once an experimental estimate of  $S$  is found it is claimed that a numerical value of  $S$  greater than  $2$  has infringed the CHSH inequality. Consequently, according to the CHSH inequality, the experiment is declared to rule out all local hidden variable theories and supports the quantum mechanics prediction.

# **3. Results**

### **3.1. Chebyshev's inequality**

**Pafnuty Chebyshev** (May 16, 1821 - December 8, 1894), a Russian mathematician, was born as a son of a wealthy landowner in the village of Okatovo, a small town in western Russia, west of Moscow. Chebyshev is known for his work about the Chebyshev's inequality too.



 $p(|X - E(X)| \ge a^* \sigma(X)) \le (1 / (a^* a)).$ 

The Chebyshev inequality above can be used to proof the relationship between the hidden and nonhidden part (Barukčić 2006c) of something, f. e. of a measurable random variable.



**Proof.**

$$
p(|X_t - E(X_t)| \ge a^* \sigma(X_t)) \le (1/(a^*a))
$$
\n(1)

$$
p(\,|\,(\mathbf{h}_{t} + (\text{ not } \mathbf{h})_{t}) - E(X_{t}) \,|\geq a^{*}\sigma(X_{t})\,)\leq\,(\,1\,/\,(a^{*}a)\,)\tag{2}
$$

Our assumption is that **there are no hidden variables**, we set  $h_t = 0$ . Thus, we obtain

$$
p( | ((\mathbf{h}_{t} = \mathbf{0}) + (not \, h)_{t}) - E(X_{t}) | \ge a^{*}\sigma(X_{t}) ) \le ( 1 / (a^{*}a) ) \tag{3}
$$

$$
p(\mid ( (0) + (not h)_t) - E(X_t) \mid \ge a^* \sigma(X_t)) \le (1/(a^* a))
$$
\n(4)

$$
p(\mid (\text{not } h)_t - E(X_t) \mid \ge a^* \sigma(X_t)) \le (1/(a^*a)) \tag{5}
$$

Our assumption is that there are no hidden variables. In so far, we obtained an **identity** of the random variable  $X_t$  itself and **( not h)<sub>t</sub>**, both are the same. In other words, the not hidden or measured part of  $X_t$ is the whole  $X_t$  itself, there is nothing else, **no hidden** part. We cannot distinguish between **(not h)**<sub>t</sub> and  $X_t$  both are identical and are the same. In so far, we obtain

$$
p(\mid (X_t = (not h)_t) - E(X_t) \mid \ge a^* \sigma(X_t)) \le (1/(a^* a))
$$
\n(6)

$$
p(\mid (X_t = X_t) - E(X_t) \mid \ge a^* \sigma(X_t)) \le (1/(a^*a)) \tag{7}
$$

$$
p(\mid X_t - E(X_t) \mid \ge a^* \sigma(X_t)) \le (1/(a^*a))
$$
\n
$$
(8)
$$

In so far, Chebyshev's inequality can be used for our purposes because the same is able to say something about hidden local variables.

$$
(a^*a)^* p(|X_t - E(X_t)| \ge a^* \sigma(X_t)) \le 1
$$
\n(9)

$$
2 * (a * a) * p(|X_t - E(X_t)| \ge a * \sigma(X_t)) \le +2
$$
 (10)

Eq. (10) times (-1) yields Eq. (11).

$$
-(2 * (a * a) * p(|X_t - E(X_t)| \ge a * \sigma(X_t))) \ge -2
$$
\n(11)

In general, we obtain the Eq. (12).

$$
-2 \le | (2 * (a * a) * p( | X_t - E(X_t) | \ge a * \sigma(X_t))) | \le +2
$$
 (12)

**Q. e. d.**

The Chebyshev's inequality is proofed and known as correct. If the CHSH inequality is true, correct and valid, then there should not be a contradiction between

$$
-2 \leq (E(a, b) - E(a, b') + E(a', b) + E(a' b')) \leq +2
$$

and

$$
-2 \leq | (2 * (a * a) * p( | X_t - E(X_t) | \geq a * \sigma(X_t) ) ) | \leq +2.
$$

However, it seems reasonable to suppose that there will be a contradiction. Consequently, in this case, it would be difficult to advocate the CHSH inequality further. According to Chebyshev's inequality it is

$$
p(|X_t - E(X_t)| \ge 2^* \sigma(X_t)) \le (1/4).
$$

In so far,  $2*\sigma(X_t)$  seems to be the point of no return in nature, the point where hidden changes into nonhidden, where matter changes into antimatter, where healthy becomes ill and vice versa.

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### **3.2. Heisenberg's uncertainty principle**

**Heisenberg uncertainty principle** or the Heisenberg indeterminacy principle ( Niels Bohr ) was discovered by Werner Heisenberg in 1927 and states in general that increasing the accuracy of the measurement of one quantity (**non - hidden** part of a random variable) increases the uncertainty of the simultaneous measurement of its other quantity, its complement, its negation (the **hidden part** of the same random variable). Let us assume, that Heisenberg uncertainty relations provides a quantitative relationship between the uncertainties of the hidden and non-hidden part of the same random variable. One fundamental consequence of the Heisenberg Uncertainty Principle is thus that it can be used to proof whether the CHSH inequality is correct.

 $L_{\text{et}}$ 



**Proof.**

$$
(\mathbf{h})_{t} \leq (\mathbf{not}\,\mathbf{h})_{t} \tag{13}
$$

$$
((h)_{t})^{2} \leq ( (not h)_{t})^{2}
$$
 (14)

$$
E((h)_{t}) \leq E((not h)_{t}) \tag{15}
$$

$$
E((h)_{t})^{2} \leq E((\text{not } h)_{t})^{2}
$$
 (16)

$$
E(((h)_{t})^{2}) \leq E(((not h)_{t})^{2}) \tag{17}
$$

$$
E(((h)_{t})^{2}) - E((h)_{t})^{2} \leq E(((not h)_{t})^{2}) - E((h)_{t})^{2}
$$
\n(18)

According to Eq. (16) we substitute E(( h)<sub>t</sub>)<sup>2</sup> by E( (not h)<sub>t</sub>)<sup>2</sup>.

$$
E(((h)_t)^2) - E((h)_t)^2 \le E(((not h)_t)^2) - E((not h)_t)^2 \tag{19}
$$

$$
\sigma((h)_t)^2 \leq \sigma((\text{not } h)_t)^2 \tag{20}
$$

Recall that  $\sigma((h)_t) \ge 0$  or  $\sigma((\text{not } h)_t) \ge 0$ .

$$
\sigma(\ (h \ )_t) \qquad \leq \qquad \sigma(\ (\text{not } h \ )_t \ ) \tag{21}
$$

According to Eq.  $(19)$ ,  $(20)$  and  $(21)$  we obtain Eq.  $(22)$ .

$$
E(((h)_t)^2) - E((h)_t)^2 \le \sigma((\text{not } h)_t)^* \sigma((\text{not } h)_t)
$$
\n(22)

According to Eq. (21) it is  $\sigma((h)_t) \leq \sigma((\text{not } h)_t)$ . We obtain Eq. (23).

$$
E(((h)_{t})^{2}) - E((h)_{t})^{2} \leq \sigma((h)_{t}) \ast \sigma((\text{not } h)_{t}) \qquad (23)
$$

$$
E((h)_{t} - E(h)_{t})^{2} \leq \sigma((h)_{t})^{*} \sigma((\text{not } h)_{t}) \qquad (24)
$$

$$
E((h)_t - E(h)_t)^* ((h)_t - E(h)_t) \le \sigma((h)_t)^* \sigma((\text{not } h)_t)
$$
 (25)

We use Eq. (13) and Eq. (15) and obtain Eq. (26).

$$
E(\ (h)_t - E(h)_t )^* (\ (not h)_t - E(\,not h)_t ) \leq \sigma(\ (h)_t )^* \sigma(\, (not h)_t ) \tag{26}
$$

On the left side of the Eq. (26) we obtained the covariance.

$$
\sigma\left(\ (h)_{t}\ ,\ (not\text{th})_{t}\ \right)\ \leq\ \sigma\left(\ (h)_{t}\ \right)\ast\sigma(\ (not\text{th})_{t}\ )\tag{27}
$$

Set  $\sigma((h)_t) > 0$  or  $\sigma((\text{not } h)_t) > 0$ .

$$
(\sigma((h)_t, (\text{not } h)_t) / (\sigma((h)_t)^* \sigma((\text{not } h)_t))) \leq +1
$$
 (28)

$$
2^* (\sigma (\ (h)_t , (\text{not } h)_t ) / (\sigma ((h)_t )^* \sigma ((\text{not } h)_t ) ) ) \leq +2
$$
 (29)

Eq. (28) time (-1) yields Eq. (29).

$$
-2 * ( \sigma ( (h)_t , (not h)_t ) / ( \sigma ( (h)_t ) * \sigma ( (not h)_t ) ) ) \geq -2
$$
 (30)

 $-2 \leq | 2 * ( \sigma ( ( h )_{t} , ( \text{not } h )_{t} ) / ( \sigma ( ( h )_{t} ) * \sigma ( ( \text{not } h )_{t} ) ) ) | \leq +2$  (31)

# **Q. e. d.**

According to Barukčić (Barukčić 2006c, pp. 15-16), we know that  $\sigma$  (( h )<sub>t</sub>, ( not h )<sub>t</sub> ) = 0 if ( h )<sub>t</sub> has nothing to do with (not h)<sub>t</sub>, if both are absolutely independent from each other, each outside the sphere of its other. In this case we obtain

$$
-2 \leq | 2 * ( 0 / ( \sigma ( (h)_t ) * \sigma ( (not h)_t ) ) ) | \leq +2
$$

Heisenberg uncertainty relations is known to be  $(\sigma((h)_t)^* \sigma((not h)_t)) \ge (h/(4*\pi))$ . In so far if there is a relation between a hidden and non-hidden part of the same random variable then it has to be at least that  $|\sigma((h)_t,(\text{not } h)_t)| \ge 0$ . On the other hand, if relation between a hidden and non-hidden part of the same random variable is constituted by Heisenberg's uncertainty relation then equally is must be true that

$$
- \, 2 \ \leq \ \mid \ 2 * ( \ h \ / (4 * \pi * \sigma ( \ ( \ h \ )_t \ ) * \sigma ( \ ( \text{not} \ h \ )_t \ ) \ ) \ \mid \ \leq + \, 2
$$

or

 $- 2 * \sigma(\text{ (not h)}_t) \leq | 2 * (\text{ h} / (4 * \pi^* \sigma(\text{ ( h })_t))) | \leq + 2 * \sigma(\text{ (not h)}_t)$  (32) or  $- 2 * \sigma ( \text{ (not h)}_t ) \le | ( h / ( 2 * \pi * \sigma ( ( h )_t ) ) ) | \leq + 2 * \sigma ( \text{ (not h)}_t )$ 

**Dirac's constant** is known to be  $\hbar = h/(2 * \pi)$ . Thus we obtain

$$
-2*\sigma(\pmod{h}_t) \leq |(\hbar/\sigma((h)_t) | \leq +2*\sigma((\rho\nu h)_t).
$$

Why should the CHSH inequality be not compatible with the equations derived on this page f. e. like

 $-2 \le | (\hbar / (\sigma((h)_t))^* \sigma((\hbar)(h_1)^*)) | \le +2.$  (33)

#### **3.3. Unified field equation**

The unified field equation cannot be free of the relation between the hidden local variable and nonhidden local variable of something.

**Unified field equation and hidden and non-hidden variable.**

Let *Rab* denote the Ricci tensor, *R* denote the Ricci scalar, *gab* denote the metric tensor, *T<sub>ab</sub>* denote the stress-energy tensor, h denote Planck's constant,  $h \approx (6.626\,0693\,(11))$   $* 10^{-34}$  [ J  $* s$  ],  $\pi$  denote the mathematical constant  $\pi$ , also known as **Archimedes' constant.** The numerical value of  $\pi$  truncated to 50 decimal places is known to be about  $π ≈ 3.14159 26535 89793 23846 26433 83279 50288 41971 69399 37510.$ *c* denote the speed of all electromagnetic radiation in a vacuum, the speed of light, where *c =* **299 792 458 [m / s],** γ denote Newton's gravitational 'constant', where  $\gamma \approx (6.6742 \pm 0.0010) * 10^{-11} [m^3 / (s^2 * kg)],$ 

> Einstein's field equation describes how a field or energy (or matter) and time changes space and vice versa. Einstein's basic field equation (EFE) is usually written in the form  $((( 4 * 2 * \pi * \gamma) * T_{ab}) / ( c^4) ) + (( R * g_{ab}) / 2 ) ) = ( R_{ab}).$

> > The unified field equation is derived (Barukčić 2006f) as

$$
((( 4 * 2 * \pi * \gamma) * T_{ab}) / ( c^4) ) * (( R * g_{ab}) / 2 ) ) \leq ((R_{ab}) * (R_{ab})) / 4.
$$

**then**

$$
-2 \leq (2^*4^*(( (4^*2^*\pi^*\gamma)^*\mathrm{T}_{ab})/(c^4))^*((R^*g_{ab})/2))/((R_{ab})^*(R_{ab})) \leq +2
$$

**Proof.** Eq. (2) Eq. (

$$
(((4^*2^*\pi^*\gamma)^*\mathrm{T}_{ab})/(c^4))^*((\mathrm{R}^*g_{ab})/2))) \le ((R_{ab})^*(R_{ab}))/4
$$
\n(34)

Let us assume that a division by  $((R_{ab})^*(R_{ab}))$  is allowed. If the division by  $((R_{ab})^*(R_{ab}))$  is not allowed, we set  $((R_{ab})^*(R_{ab})) = 1$ .  $4^*((((4^*2^*\pi^*\gamma)^*\mathrm{T}_{ab})/(c^4))^*((R^*g_{ab})/2)))(((R_{ab})^*(R_{ab})) \leq +1$  (35)

$$
(2 *4*)((((4 *2* \pi^* \gamma)^* \mathrm{T}_{ab})/(c^4))^*((\mathrm{R}^* \mathrm{g}_{ab})/2))) / ((R_{ab})^* (R_{ab})) \leq +2
$$
 (36)

Eq. (36) times (-1) yields Eq. (37).

$$
-(2 *4 * (((4 *2 * \pi * \gamma) * T_{ab})/(c^4)) * ((R * g_{ab})/2))) ((R_{ab}) * (R_{ab}))) \ge -2
$$
 (37)

At the end we obtain Eq. (38).

$$
-2 \leq | (2 * 4 * (((4 * 2 * \pi^* \gamma) * T_{ab})/(c^4)) * ((R * g_{ab})/2))) / ((R_{ab}) * (R_{ab})) | \leq +2
$$
 (38)

**Q. e. d.**

Why should the CHSH inequality be not compatible with Einstein's field equation and the unified field equation? This is a very precise inequality. If there is a problem between locality in General Relativity and in Quantum Mechanics, then this inequality must be violated.

#### **3.4. Natura facit saltus in general**

The quantitative alteration of  $X_t$  and Anti  $X_t$  is not at the same time identical with the creation of a new something, a new quality. The quantitative alteration of  $X_t$  and Anti  $X_t$  remains to some extent indifferent to this quantitative alteration. The relationship between  $X_t$  and Anti  $X_t$  is determined by the fact, that there is a point, where this quantitative alteration of both shows itself as specifying, **natura facit saltus**, something new is created, the altered  $X_t$  and Anti  $X_t$  are converted into a new something. The transition of  $X_t$  and Anti  $X_t$  into something new is a leap. In this new, the difference of  $X_t$  and Anti  $X_t$  has found its own completion ( Hegel 1988, p. 424 ). If there is something like a hidden local variable and a nonhidden local variable of the same something then there must be a relation to the general contradiction law (Barukčić, 2006e) too.

#### **Natura facit saltus in general.**

 $\mathbf{L}$ 



**Then**

$$
-2 \leq | (2^*4^*(X_t * (Anti X)_t) / C_t^2) | \leq +2.
$$

**Proof.**

$$
X_t^* (Anti X)_t \le C_t^2/4 \tag{39}
$$

Let us assume, that a division by  $C_t^2$  is allowed and possible.

$$
4^*(X_t^* (Anti X)_t)/C_t^2 \le 1
$$
\n(40)

$$
((2^*4^*(X_t*(\text{Anti }X)_t)) / C_t^2) \leq +2
$$
 (41)

$$
-((2*4*(Xt*(Anti X)t))(Ct2) \ge -2
$$
\n(42)

$$
-2 \leq |((2^*4^*(X_t * (Anti X)_t)) / C_t^2)| \leq +2
$$
 (43)

**Q. e. d.**

Why should the CHSH inequality be not compatible with the inequality (43) derived from the general contradiction law?

#### **4. Discussion**

This publication has shown that the CHSH inequality has been given at least a very imprecise definition of the relation between the hidden and non-hidden part of something. In other words, the CHSH inequality is not deeply connected with Einstein's and Heisenberg's understanding of the physical sciences. Roughly speaking, the explanatory ambitions of the CHSH inequality are more or less not based on basic and secured scientific findings.

Experiments based on the inequalities derived and proofed in this publication should be able to proof the opposite of the CHSH inequality.

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